## Multiformalism modeling

# An introduction to multiformalism modeling for performance evaluation

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1st ECMS International School for Young Researchers Politechnika Krakowska, 3/6/2024





#### What will we do today?

- What is performance modeling? Why do we use it?
- Examples: Queuing Networks, Stochastic Petri Nets
- Multiformalism modeling

## **Performance modeling**

- *Performance Evaluation* is the quantitative and qualitative study of systems, to evaluate, measure, predict and ensure target behaviors and performances
- It is usually carried on using *models of a system*
- A model is an abstraction of a system:

"an attempt to distill, from the details of the system, exactly those aspects that are essentials to the system behavior"....

(E. Lazoswka)

- After a model has been defined, it is usually exploited in three steps:
  - Validation
  - Projection
  - Verification

## **Performance modeling**

- During the *validation* phase, results predicted by the model are compared against measurement of the real system to check if they match
- The *projection* changes some of the parameters of the model (i.e. the speed or the quantity of a component) and computes the corresponding indices to see if a goal is met in the new configuration
- *Verification* actually modifies the real system according to the new parameters tested in the model, to check whether the objective has been really achieved

## Solution techniques

- Once a model has been defined, its performance indices are computed using suitable solution techniques. Different procedures exists, and the most common are:
  - *Analytical* and *numerical* techniques are based on the application of mathematical techniques, which usually exploit results coming from the theory of probability and stochastic process
    - If the technique uses expressions in closed form (i.e. a formula or an exact algorithm to compute them can be derived), it is said to be *analytical*
    - If the solutions can only be obtained using numerical procedures, the techniques are said to be *numerical*
  - Simulation is based instead on the reproduction of *traces* of the model
    - A trace is a possible sequence of events that can characterize one possible evolution of the model



## A problem with arrivals and departures

• Let us observe an abstract system, where we can only focus on its entry and exit point, for a given amount of time *T* 



By simply counting the jobs that enters and leaves the system in the considered time frame, we can determine its main parameters (*arrival rate* and *average service time*), and performance indices (*utilization, throughput, average service time, average number of jobs in the system*)

### **Example: Queuing Networks**

- *Queuing Networks* represent systems using a set of interconnected entities called queues
- Born in the TLC domain, they are widely adopted whenever queuing effects impact on system performances



## Queuing stations

- *Queuing stations* can be used to model several elements of a system:
  - CPUs in multi-tasking S.O., disks, web services, communication channels, routers with buffers
  - Manufacturing machines
- Queues are populated by entities that require services
- Depending on the context, such entities are called customers, clients, jobs, tasks, packets, tokens, ...
- Stochastic characterization of service times and arrival rates
- Evaluation of the stability conditions
- Strong mathematical foundations allow analytical evaluation, event-based simulation as alternative

#### Open and closed networks

- Queuing networks can be either *open* or *closed* 
  - In open models jobs arrive from outside at a specified arrival rate
  - In *closed models* there is a fixed population of jobs that moves between the queues inside the system
- Open Models are characterized by *arrivals* and *departures* from the system
- In closed models we
  have a fixed population
  of Njobs that
  continuously circulate
  inside the system



### **Performance indices**

- From a service station, several performance indices can be computed, depending on the problem
- The most important are:
  - the *utilization*: is the fraction of time a server is busy (not waiting for new jobs to arrive)
  - the *response time*: is the average time spent by a job at a service center
  - the *average queue length*: accounts for the mean number of jobs in a service station (both the ones being served and the ones in the queue)
  - the *throughput*: describes the rate at which jobs are served and depart from the station

## Network performance indices

- On network models, extra performance indices can be defined:
  - System throughput
  - Total system population
  - System response time
- For what concerns utilization, there is no unique definition of a system-wise measure:
  - The fraction of time in which there is at least one job in the system
  - The average utilization of all the stations
  - The utilization of the bottleneck station
- All definitions have strength and weaknesses

## **Example: Stochastic Petri Nets**

- Queuing networks are perfect to model systems where jobs are executed through a set of stations
- They are characterized by convenient high-level performance indices such as throughput, response times and utilization
- However, they cannot easily model *resource contentions* and *concurrency*
- Other formalisms, such as *Stochastic Petri Nets*, are used to model systems characterized by such features

#### Petri Nets

• Petri Nets are *bi-partite graphs*, characterized by two set of elements: *places* and *transitions* 



## Petri Nets performance models

- The meaning of the different type of arcs is the following:
  - *input arcs* model *preconditions*, that must be satisfied for an event to take place
  - *output arcs* are used to specify the *effect* of the actions
  - *inhibitor arcs prevent* an event from taking place
- In performance models created using Petri nets, tokens are used to represent jobs, places to define queues or resource occupancy, and transitions correspond to services





#### **Enabled transitions**

- A transition is said to be enabled if:
  - Each input place has at least as many token as the weight of the corresponding input arc
  - Each place connected with an inhibitor arc has less tokens than the weight of the connection



#### Firing time distribution

- The original definition of *Stochastic Petri Net*s, associate to each transition an *exponentially distributed random* firing time
- Extended models, called *Non-Markovian Stochastic Petri Nets*, allow to use general firing time distributions
- Conflict are solved with a *race policy*: the system will evolve according to the transition that will fire first

#### Performance indices: transition throughput

- Only three types of performance indices are defined on PNs
  - the transition throughput counts the average number of firings per time unit done by a transition
  - for places, it is relevant to compute either the probability distribution of having a given number of tokens, or the average number of tokens inside it

### **Colored Petri Nets**

• In *Colored Petri Nets*, tokens are divided into classes called *colors*: each place might contain a different number of tokens for each color



#### Modeling complex systems

• Problem: modern complex systems have *different aspects* related to *different domains* and *different expertise* but must be represented and evaluated as a whole

•

**ETCS** 



Fig. 4. ERTMS/ETCS system

## Multiformalism models

- Multiformalism models allows to exploit different formalisms to describe different components of a system
- They can use the *most appropriate modelling primitive* for each part, and can combine different modeling languages
- One of the main advantages of multi-formalism modelling is its ability to represent the system at *multiple levels of abstraction*
- This allows a *more comprehensive and accurate representation* of the system, which can *facilitate the analysis* and optimization of the behavior of the system

#### **Definition and challenges**

- "Multi-formalism modeling is the combination of different formalisms, such as Petri nets, process algebras, and queuing networks, to capture different system behaviours and characteristics"
- Main problems: semantics, analysis, representation, modularity/compositionality, coherence

#### Example of a simple multiformalism model

- One of the most popular example of multiformalism modeling technique is the combination of Queuing Networks and Petri Nets
- If a transition is connected to a queue, whenever the transition fires, it inserts as many jobs as the weight of its arc in the destination queue
- The class of the jobs corresponds to the color of the tokens



#### **Example: architecture**

- The lineside subsystem: it is mainly responsible for providing geographical position information to the on-board subsystem;
- The on-board subsystem: it is the core of the control activities located on the train;
- The trackside subsystem: it is in charge of monitoring the movement of the trains.



Fig. 1. ERTMS/ETCS architecture

## Example: UML component diagrams







#### Example: scenario components



Fig. 5. Contributions of the different sub-models to the overall analysis

#### **Example: reliability**





#### **Example: performability**



Fig. 9. The structure of the GSPN performability model











Fig. 12. On-board timing module in vital communication model

#### So what?

- We analyzed the different submodels for the different aspects of the system
- All submodels showed compliance with specifications and expected system behavior
- The overall multiformalism system analysis showed that there is a possibility of system failure with no component failure because of combined effects of a legitimate combination of delays of computing and transmissions and a misinterpretation by the control logic
- Such a problem is a *higher level system effect* not trackable to any of the logs of the components, which show absolutely no error

## **Doing multiformalism**

- What do we need to use multiformalism modeling?
  - Proper model composition tools
  - Proper model analysis strategies
  - Proper model analysis tools
  - A novel theoretical approach

#### Tools to define multi-formalism models



#### DrawNet++: a Flexible Framework for Building Dependability Models

G. Franceschinis, M. Gribaudo, M. Iacono, V. Vinorini, C. Benoncelio 5

#### 1. DrawNet++ quick overview and context

The DuseNetia project addresses the compositional construction of dependability models [3, 4]. Its main goals are to provide, as a GUI to any graph-based formation; b) a support is the design process of dependability models, according to scoreging improves of the defendability models, according to scoreging improve by object orientization (OD); (4) a user framily, three-and for defenda classes of analy six/stransfer body.

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#### 2. DrawNet++ demonstration

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Figure 1. A PFT example

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#### Multi-solution by orchestration



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- Multiformalism potential is not limited to a joint analysis of heterogeneous submodels
- In the Mobius approach a superformalism towards which all formalisms are translated allow the generation of a single analysis model
- In the SIMTHE*Sys* approach *elements from different formalisms may actually natively interact* by specifying their elementary interactions and complex state change conditions, to account for actual behaviors of a system

- The main idea was finding an object-oriented way of describing the interactions between modelling primitives
- The abstraction offered by OOP could immediately define an interconnection semantic between primitives of different formalisms



• A closed system, with servers that can break and repair, together with the possibility of transferring a job to a secondary system in case of long waits



• The proposed rules allow either to produce a Continuous Time Markov Chain for numerical analysis, or to compute a solution using discrete events simulation



#### Other interesting cases

- Specifying complex verification properties
  - Petri nets to specify behaviors, Fault Trees to evaluate conditions, automata to assess properties
- Modeling the effects of software rejuvenation policies
  - Combining a traditional modelling language with a *Domain Specific Language* properly defined to represent alternate software rejuvenation policies
- Hybrid systems
  - Modeling systems with continuous time and discrete time components

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Exploiting multiformalism models for testing an

#### Introduction and related works

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## **Rethinking PN/QN connections**

- We defined non-traditional PN/QN connections
- We started considering possible applicative scenarios of the connections, aiming at making models "readable"



Fig. 2. Advanced connection types: queue to transition and place to queue.

- Eviction
- Failure
- Time-Out

















Fig. 4. Advanced connection types: exclusive connection from place to queue and from queue to transition.



- · On / Off / Enabling / disabling
- · Server reduction









Fig. 5. Advanced connection types: from several queues directly to a timed or immediate transition.

Fig. 3. Advanced connection types: test and inhibitor arcs.

Places, Transitions and Oursee

Introduction

## Rethinking PN/QN connections

- We tried to test different semantics, in a simple goods delivery model
- These semantic focused on differences between jobs in service and waiting in the queue



## Rethinking PN/QN connections

- We showed that the different semantics have a strong impact on the performance measures that can be computed on the models:
  - they cannot be simply ignored, or left unspecified!



#### **Questions?**

The ERTMS/ETCS running example models are from Francesco Flammini, Stefano Marrone, Mauro Iacono, Nicola Mazzocca, Valeria Vittorini, A Multiformalism Modular Approach to ERTMS/ETCS Failure Modelling. International Journal of Reliability, Quality and Safety Engineering, vol. 21, num. 1, pp. 1450001-1-1450001-29, World Scientific, ISSN: 0218-5393, DOI: 10.1142/S0218539314500016

My gratitude goes to my friend prof. Marco Gribaudo for 25 years of work together and for providing part of the materials used in this presentation

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